

Intervention for Algebra I

Module 1: Student Booklet





The Meadows Center
FOR PREVENTING EDUCATIONAL RISK
THE UNIVERSITY OF TEXAS AT AUSTIN
COLLEGE OF EDUCATION

Mathematics Institute for Learning Disabilities and Difficulties

www.meadowscenter.org

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Engage Prior Knowledge Practice

Brainstorm

List symbols that are used in mathematics.

Demonstration Practice

Determine whether each of the following situations represents an example of a variable or a nonexample of a variable. Circle "Example" or "Nonexample" and justify your reasoning in the space provided.

1. $1 \text{ g} = 1,000 \text{ mg}$

Example or Nonexample

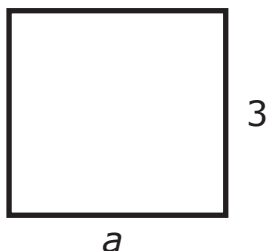
Because _____

2. $3x - 1 = y$

Example or Nonexample

Because _____

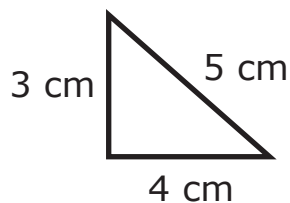
3.



Example or Nonexample

Because _____

4.



Example or Nonexample

Because _____

P practice

Activity 1: Guided Practice

Determine whether each of the following situations represents an example of a variable or a nonexample of a variable. Circle "Example" or "Nonexample" and justify your reasoning in the space provided.

$$3^3 \geq 25$$

Example or Nonexample

Because there are no symbols that represent 1 value or set of values

1. $5 \text{ m} = 500 \text{ cm}$

Example or Nonexample

Because _____



Example or Nonexample

Because _____

3. $V = \frac{100}{p}$

Example or Nonexample

Because _____

P

ractice (cont.)

Activity 2: Pair Practice

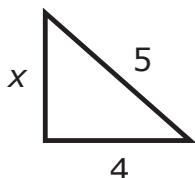
Work with your partner to determine whether each of the following situations represents an example of a variable or a nonexample of a variable. Circle "Example" or "Nonexample" and justify your reasoning in the space provided.

$$5x - 1 = 13$$

Example or Nonexample

Because the variable "x" represents 1 value in the equation

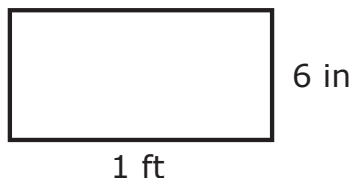
1.



Example or Nonexample

Because

2.



Example or Nonexample

Because

3. 100 cm = 1 m

Example or Nonexample

Because

Name: _____

I

ndependent Practice

Score: ____ / 11 correct

1. Fill in the blank with the correct term. (1 pt.)

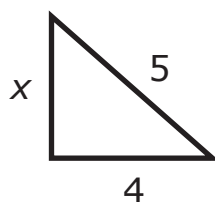
A _____ is a symbol, usually a letter, that represents 1 value or set of values.

2. Determine whether each of the following situations represents an example of a variable or a nonexample of a variable. Circle all examples and cross out all nonexamples. Be prepared to justify your answer. Each situation is worth 1 point.

Example

~~Nonexample~~

$$1 \text{ m} = 0.001 \text{ km}$$

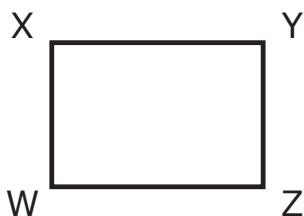


$$p \geq 13$$

$$15(p) - 7 = 2$$

$$24 \text{ in} = 2 \text{ ft}$$

$$4^3 = 64$$



$$22 + 3m = -4$$

$$2 \text{ g} = 200 \text{ cg}$$

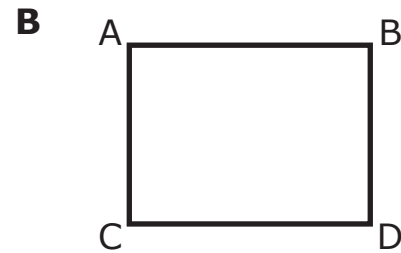
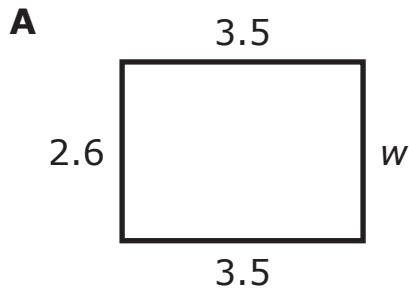
$$\sqrt{9} = 3$$

Cumulative Review Practice

Score: ____ / 2 correct

For each question, circle the letter of the correct response.

1. An example of a variable is (1 pt.)

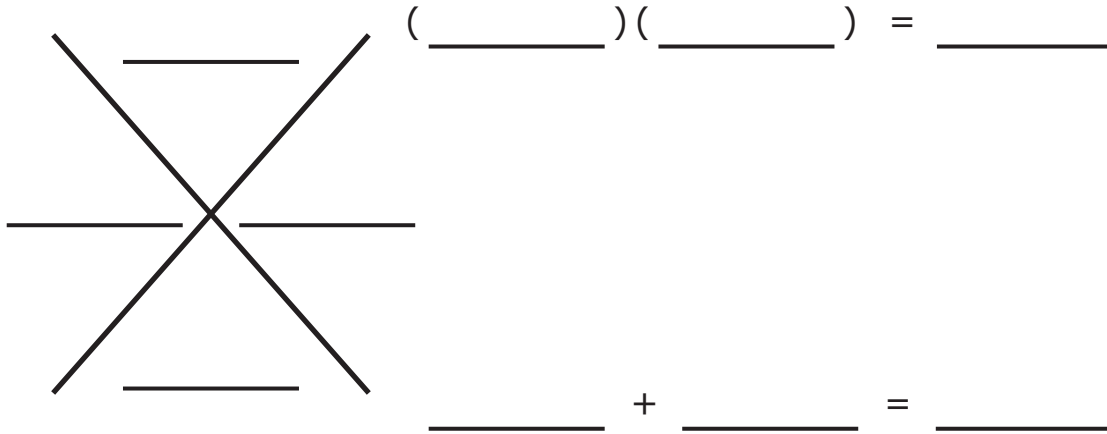


2. A situation that does not use a variable is (1 pt.)

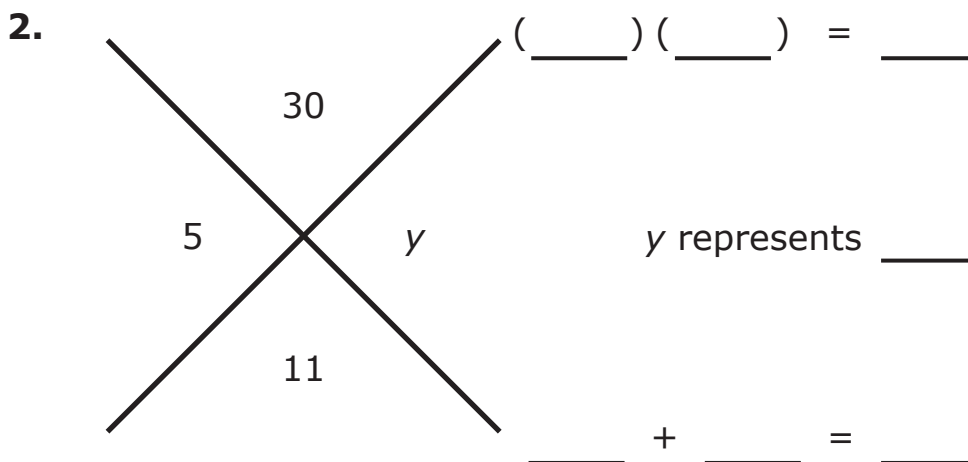
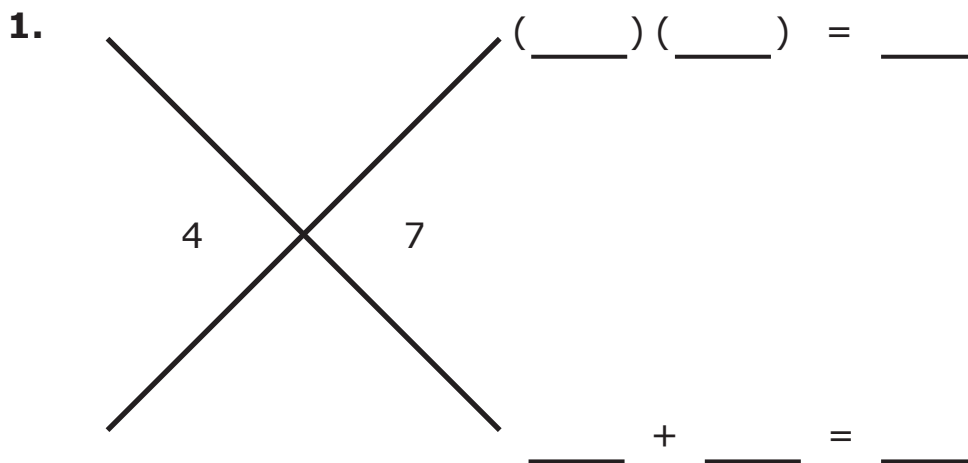
A $3(p)^2 + 8 - \frac{10}{2}$

B $\{(7 + 1)^2 - 9\} + 4$

Demonstration Practice

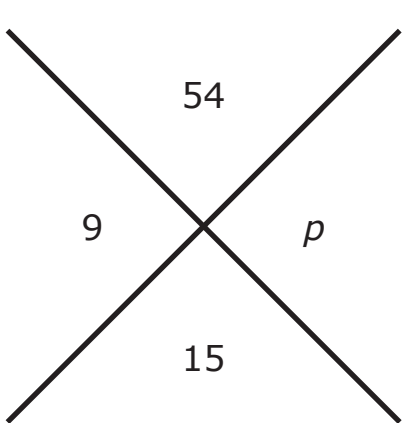


For the following number puzzles, write the equations and determine the missing values for the fixed unknown variables.



Demonstration Practice (cont.)

3.

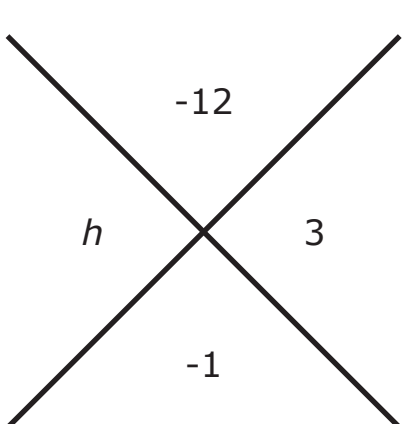


$(\quad)(\quad) = \quad$

p represents \quad

$\quad + \quad = \quad$

4.



$(\quad)(\quad) = \quad$

h represents \quad

$\quad + \quad = \quad$

P practice

Pair Practice

With your partner, for each of the following number puzzles, determine what the fixed unknown variable represents.

1. Determine the value for the variable that is a fixed unknown.

$$\begin{array}{c}
 \diagup 64 \diagdown \\
 8 \quad g \\
 \diagdown 16 \diagup
 \end{array}
 \quad
 \begin{array}{l}
 (\quad)(\quad) = \quad \\
 \quad + \quad = \quad
 \end{array}$$

The variable g represents _____

2. Determine the value for the variable that is a fixed unknown.

$$\begin{array}{c}
 \diagup 24 \diagdown \\
 4 \quad h \\
 \diagdown 10 \diagup
 \end{array}
 \quad
 \begin{array}{l}
 (\quad)(\quad) = \quad \\
 \quad + \quad = \quad
 \end{array}$$

The variable h represents _____

3. Determine the value for the variable that is a fixed unknown.

$$\begin{array}{c}
 \diagup -25 \diagdown \\
 a \quad 5 \\
 \diagdown 0 \diagup
 \end{array}
 \quad
 \begin{array}{l}
 (\quad)(\quad) = \quad \\
 \quad + \quad = \quad
 \end{array}$$

The variable a represents _____

Error Correction Practice

The given situations are work completed by two different students.
Determine which student is incorrect and explain the error.

Question:

For the following equations, determine the value of the fixed unknown variable.

$$\begin{aligned} 6h &= 24 \\ 6 + h &= 10 \end{aligned}$$

Student 1

$$\begin{aligned} 6h &= 24 & 6 + h &= 10 \\ \frac{6h}{6} &= \frac{24}{6} & -6 & \quad -6 \\ h &= 4 & h &= 4 \end{aligned}$$

Student 2

$$\begin{aligned} 6h &= 24 & 6 + h &= 10 \\ -6 & \quad -6 & -6 & \quad -6 \\ h &= 18 & h &= 4 \end{aligned}$$

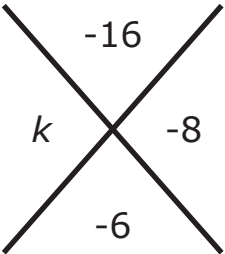
Name: _____

I

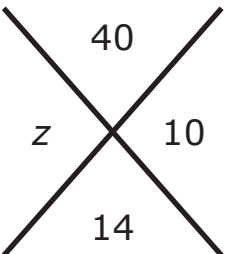
ndependent Practice

Score: ____ / 3 correct

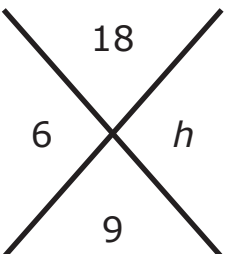
For each of the following number puzzles, determine the value of the fixed unknown variable that makes the puzzle true. Each puzzle is worth 1 point.

1.  (____)(____) = ____
____ + ____ = ____

The variable k represents ____

2.  (____)(____) = ____
____ + ____ = ____

The variable z represents ____

3.  (____)(____) = ____
____ + ____ = ____

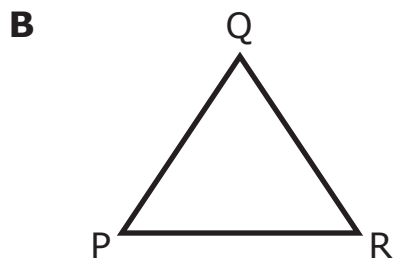
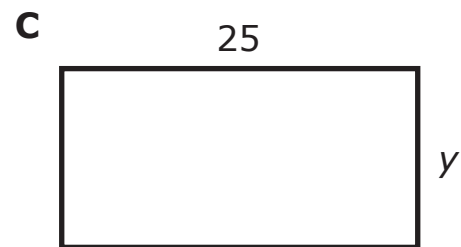
The variable h represents ____

Cumulative Review Practice

Score: ____ / 4 correct

1. Determine which of the following situations is an example of a variable. For each item, circle the letter of the correct response. (1 pt.)

A $1,000 \text{ g} = 2.2 \text{ lb}$



D $81 < 10^2$

2. For the following problem, determine the value that makes the number puzzle true.

$(\underline{\hspace{1cm}})(\underline{\hspace{1cm}}) = \underline{\hspace{1cm}}$ (1 pt.)

$\underline{\hspace{1cm}} + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$ (1 pt.)

The variable b represents _____ (1 pt.)

Demonstration Practice

The following equations represent a pattern. Determine the pattern for each set of equations and use variables to write a generalization of the pattern.

1. $2(1) = 2$ Check your generalization.
 $3(1) = 3$
 $4(1) = 4$
 $5(1) = 5$

In each equation we _____

_____.

The variable _____ represents _____

because _____

_____.

The generalization for this pattern is _____

In other words: _____

2. $6 - 6 = 0$ Check your generalization.
 $7 - 7 = 0$
 $8 - 8 = 0$

In each equation we _____

_____.

The variable _____ represents _____

because _____

_____.

The generalization for this pattern is _____

In other words: _____

Demonstration Practice (cont.)

3. $\frac{2}{1} = 2$

Check your generalization.

$\frac{4}{1} = 4$

$\frac{8}{1} = 8$

In each equation we _____
_____.

The variable _____ represents _____

because _____
_____.

The generalization for this pattern is _____

In other words: _____

P practice

Pair Practice

The following equations represent a pattern. With your partner, determine the pattern for each set of equations and match to the correct generalization equation.

Pattern Equations

Generalizations

1. $-2(0) = 0$
 $-1(0) = 0$ _____
 $5(0) = 0$

A $a(1) = a$

B $b(0) = 0$

2. $7 - 7 = 0$
 $8 - 8 = 0$ _____
 $15 - 15 = 0$

C $\frac{c}{1} = c$

D $d - d = 0$

3. $-4(1) = -4$
 $3(1) = 3$ _____
 $8(1) = 8$

4. $\frac{-2}{1} = -2$
 $\frac{0}{1} = 0$ _____
 $\frac{2}{1} = 2$

Error Correction Practice

The given situations are work completed by two different students.
Determine which student is incorrect and explain the error.

Question:

Write the equation that represents the generalization from the set of
numeric equations.

$$-3 + 0 = -3$$

$$-1 + 0 = -1$$

$$1 + 0 = 1$$

$$3 + 0 = 3$$

Student 1

$$-x + 0 = x$$

Student 2

$$x + 0 = x$$

Name: _____

Independent Practice

Score: _____ / 4 correct

Determine the pattern for each set of equations and match to the correct generalization equation. Each match is worth 1 point.

Pattern Equations

Generalizations

- | | | |
|----|---------------|-------|
| | $10 + 0 = 10$ | |
| 1. | $20 + 0 = 20$ | _____ |
| | $35 + 0 = 35$ | |
| | $3(1) = 3$ | |
| 2. | $4(1) = 4$ | _____ |
| | $11(1) = 11$ | |
| | $4 - 4 = 0$ | |
| 3. | $7 - 7 = 0$ | _____ |
| | $9 - 9 = 0$ | |
| | $-7(0) = 0$ | |
| 4. | $15(0) = 0$ | _____ |
| | $-8(0) = 0$ | |

A $m(1) = m$

B $p - p = 0$

C $h + 0 = h$

D $a(0) = 0$

Cumulative Review Practice

Score: ____ / 4 correct

1. Determine the fixed unknown value that makes the number puzzle true.

$$\begin{array}{c}
 \begin{array}{cc}
 \diagup & 66 \\
 11 & \diagdown \\
 \diagdown & n \\
 17 & \diagup
 \end{array}
 \end{array}$$

____ (____) = ____ (1 pt.)

____ + ____ = ____ (1 pt.)

The variable n represents ____ (1 pt.)

2. The following 3 equations represent a pattern. Determine the pattern.

$$\begin{array}{l}
 5 - 0 = 5 \\
 7 - 0 = 7 \\
 8 - 0 = 8
 \end{array}$$

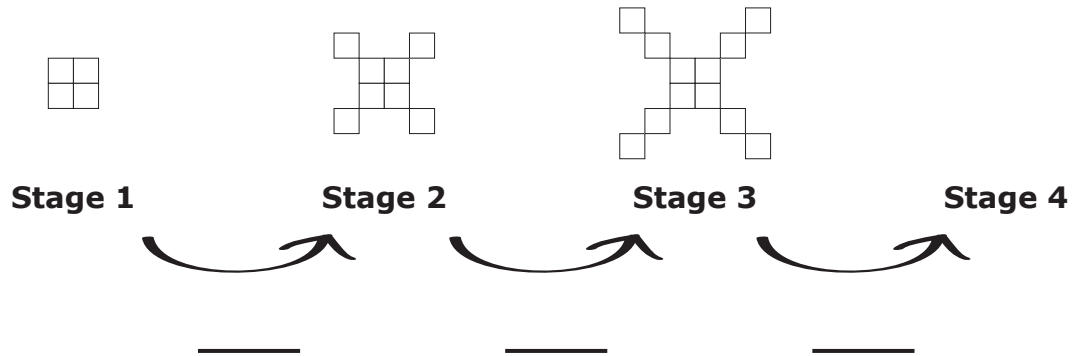
Which of the following generalizations best represents the pattern? (1 pt.)

- A** $h - 0 = h$
- B** $h + 0 = h$
- C** $h - h = 0$
- D** $h(1) = h$

Demonstration Practice

Use the pattern in the tile design to fill out each table and use a variable to write a generalization.

1.



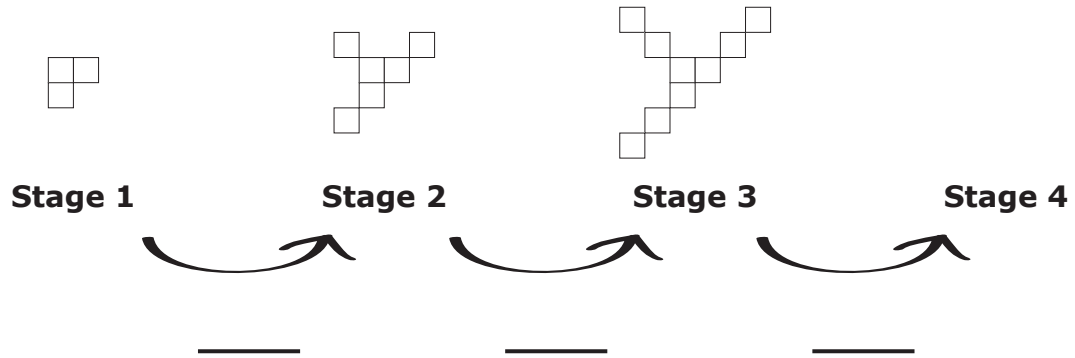
(Stage) n	Thinking Process	Total
1		
2		
3		
4		

Common Difference: _____

Generalization: _____

Demonstration Practice (cont.)

2.



(Stage) n	Thinking Process	Total
1		
2		
3		
4		

Common Difference: _____

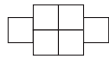
Generalization: _____

Practice

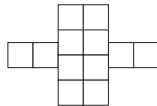
Guided Practice

Use the pattern in the tile design to fill out each table and use a variable to write a generalization.

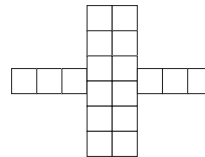
1.



Stage 1



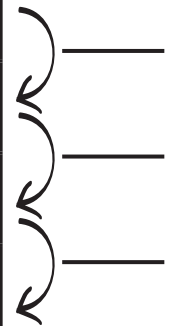
Stage 2



Stage 3

Stage 4

(Stage) n	Thinking Process	Total
1		
2		
3		
4		



Common Difference: _____

Generalization: _____

Practice (cont.)

Pair Practice

Use the pattern in the tile design to fill out each table and use a variable to write a generalization.

1.



Stage 1



Stage 2



Stage 3

Stage 4

(Stage) n	Thinking Process	Total
1		
2		
3		
4		

Common Difference: _____

Generalization: _____

Name: _____

Independent Practice

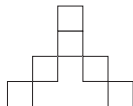
Score: _____ / 13 correct

Use the pattern in the tile design to fill out each table and use a variable to write a generalization. (13 pts.)

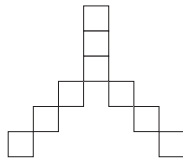
1.



Stage 1



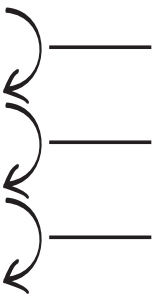
Stage 2



Stage 3

Stage 4

(Stage) n	Thinking Process	Total
1		
2		
3		
4		



Common Difference: _____

Generalization: _____

Cumulative Review Practice

Score: ____ / 2 correct

1. Determine the pattern and select the correct generalization. (1 pt.)

$$\frac{-3}{1} = -3$$

$$\frac{8}{1} = 8$$

$$\frac{13}{1} = 13$$

A $\frac{3}{1} = 3$

C $\frac{n}{1} = 1$

B $\frac{n}{1} = -n$

D $\frac{n}{1} = n$

2. Use the pattern in the tile design to fill out the table and use a variable to write a generalization of this pattern.

Stage 1



Stage 2



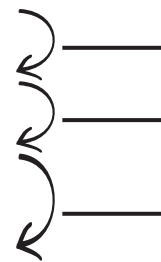
Stage 3



Stage 4



Stage	Process	Total
1	⊕ ⊕	2
2	⊕ ⊕ ⊕ ⊕	4
3	⊕ ⊕ ⊕ ⊕ ⊕ ⊕	6
4	⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕	8



Which of the following is the correct generalization for the pattern in the table? (1 pt.)

A $2n$

C $6n$

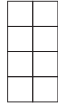
B $n + 3$

D $n + 2$

Demonstration Practice

For the following problems, determine the pattern from the table and use variables to write a generalization of the pattern.

Stage 1 Stage 2 Stage 3 Stage 4



Term	Thinking Process		Total
1	\oplus	$\text{---} (\text{---}) + \text{---}$	2
2	$\oplus \oplus \oplus \oplus$	$\text{---} (\text{---}) + \text{---}$	4
3	$\oplus \oplus \oplus \oplus \oplus \oplus$	$\text{---} (\text{---}) + \text{---}$	6
4	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus$	$\text{---} (\text{---}) + \text{---}$	8
n	--- group(s) of --- plus --- extra $\text{---} (\text{---}) + \text{---}$		



The generalization of this pattern is _____

Demonstration Practice (cont.)

2.

Term	Thinking Process	Total
1	$\oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	4
2	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	7
3	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	10
4	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	13
n	$\text{---} \text{ group(s) of } \text{---} \text{ plus } \text{---} \text{ extra } \text{---} (\text{---}) + \text{---}$	



Constant: _____

The generalization of this pattern is _____

Practice

Guided Practice

Determine the pattern from the table and use a variable to write a generalization of the pattern.

Term	Thinking Process	Total
1	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	8
2	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	13
3	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	18
4	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	23



n	--- group(s) of --- plus --- extra $\text{---} (\text{---}) + \text{---}$
-----	--

The generalization of this pattern is ---

Pair Practice

With a partner, determine the pattern from the table and use a variable to write a generalization of the pattern.

Term	Thinking Process	Total
1	<div> <div>⊕ ⊕ ⊕ ⊕ ⊕</div> <div>_____ (_____) + _____</div> </div>	5
2	<div> <div>⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕</div> <div>_____ (_____) + _____</div> </div>	9
3	<div> <div>⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕</div> <div>_____ (_____) + _____</div> </div>	13
4	<div> <div>⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕</div> <div>_____ (_____) + _____</div> </div>	17
n	_____ group(s) of _____ plus _____ extra _____ (_____) + _____	

The generalization of this pattern is

Name: _____

Independent Practice

Score: ____ / 12 correct

Determine the pattern from the table and use a variable to write a generalization of the pattern. (10 pts.)

Term	Thinking Process	Total
1	$\oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	5
2	$\oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	8
3	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	11
4	$\oplus \oplus \oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	14
n	$\text{---} \text{ group(s) of } \text{---} \text{ plus } \text{---} \text{ extra } \text{---} (\text{---}) + \text{---}$	



The generalization of this pattern is _____

Cumulative Review Practice

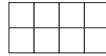
Score: ____ / 2 correct

1. Use the pattern blocks and the table below to answer the questions.

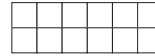
Stage 1



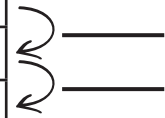
Stage 2



Stage 3



Stage	Thinking Process	Total Number of Tiles
1		4
2		8
3		12



Which of the following is the correct generalization? (1 pt.)

- A $2n$
- B $n + 8$
- C $4n$
- D $n + 4$

2. Look at the table below.

Term	Thinking Process	Total
1	$\oplus \oplus \oplus \oplus \oplus$ $(1)(3) + 2$	5
2	$\oplus \oplus \oplus \oplus \oplus$ $\oplus \oplus \oplus$ $(2)(3) + 2$	8
3	$\oplus \oplus \oplus \oplus \oplus$ $\oplus \oplus \oplus \oplus \oplus$ \oplus $(3)(3) + 2$	11
4	$\oplus \oplus \oplus \oplus \oplus$ $\oplus \oplus \oplus \oplus \oplus$ $\oplus \oplus \oplus \oplus$ $(4)(3) + 2$	14
n		??

Which of the following is the correct generalization for the pattern in the table? (1 pt.)

- A $3n$
- B $n + 5$
- C $n + 2$
- D $3n + 2$

Demonstration Practice

Determine the pattern from the table and use a variable to write a generalization of the pattern.

1.

Term	Thinking Process	Total
1	$\oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	3
2	$\oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	5
3	$\text{---} (\text{---}) + \text{---}$	7
4	$\text{---} (\text{---}) + \text{---}$	9

n	group(s) of --- plus --- extra $\text{---} (\text{---}) + \text{---}$
-----	---

The generalization of this pattern is ---

Demonstration Practice (cont.)

2.

Term	Thinking Process	Total
1	$\begin{array}{c} \oplus \oplus \oplus \oplus \\ \oplus \end{array}$ $\text{---} (\text{---}) + \text{---}$	5
2	$\text{---} (\text{---}) + \text{---}$	7
3	$\text{---} (\text{---}) + \text{---}$	9
4	$\text{---} (\text{---}) + \text{---}$	11
n		

The generalization of this pattern is _____

Practice

Pair Practice

With a partner, determine the pattern from the table and use a variable to write a generalization of the pattern.

Term	Thinking Process	Total
1	$\oplus \oplus \oplus \oplus \oplus \oplus$ $\text{---} (\text{---}) + \text{---}$	7
2	$\text{---} (\text{---}) + \text{---}$	10
3	$\text{---} (\text{---}) + \text{---}$	13
4	$\text{---} (\text{---}) + \text{---}$	16


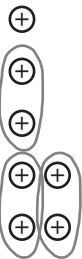

n	$\text{---} (\text{---}) + \text{---}$	
-----	--	--

The generalization of this pattern is _____

Error Correction Practice

The given situation is work completed by a student. Explain the error(s) the student made in the work.

Given the following table, write a generalization for the pattern.

Term	Process	Total
1	 $2(2) + 1$	5
2	 $3(2) + 1$	7
3	 $4(2) + 1$	9

The student circled the counters in the Process column and wrote the numeric statements.

Student conclusion:

The generalization for this pattern is $2n + 1$.

Name: _____

Independent Practice

Score: ____ / 10 correct

Determine the pattern from the table and use a variable to write a generalization of the pattern. (10 pts.)

Term	Thinking Process	Total
1	<div> <div>⊕ ⊕ ⊕ ⊕ ⊕ ⊕</div> <div>____ (____) + ____</div> </div>	7
2	<div> <div>⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕</div> <div>____ (____) + ____</div> </div>	9
3	<div> <div>____ (____) + ____</div> </div>	11
4	<div> <div>____ (____) + ____</div> </div>	13




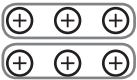
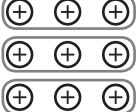
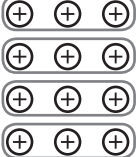
n	____ group(s) of ____ plus ____ extra ____ (____) + ____
-----	--

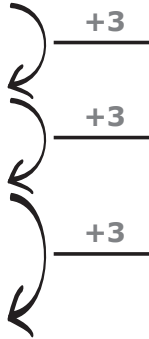
The generalization of this pattern is _____

Cumulative Review Practice

Score: ____ / 2 correct

1. Use the completed table to answer the following question.



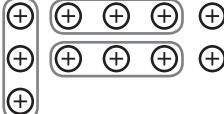

(Stage) n	Thinking Process	Total
1	 1(3)	3
2	 2(3)	6
3	 3(3)	9
4	 4(3)	12
n		??

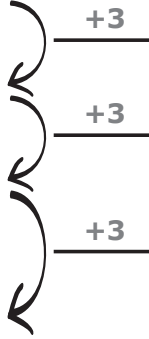


Which of the following is the correct generalization of the table's pattern? (1 pt.)

- A** $3n$ **B** $3n + 3$ **C** $n + 3$ **D** $n + 2$

2. Use the completed table to answer the following question.

(Stage) n	Thinking Process	Total
1	 1(3)+2	5
2	 2(3)+2	8
3	 3(3)+2	11
4	 4(3)+2	14
n		??



Which of the following is the correct generalization of the table's pattern? (1 pt.)

- A** $n + 1$ **B** $3n + 2$ **C** $3n$ **D** $5n + 2$

Demonstration Practice

Brainstorm:

Addition	Subtraction	Multiplication	Division	Equals

For the following situations, define the variables that are appropriate and write an equation to describe the relationship.

1. The sum of a number and 7 is 15.

Variable(s): _____

Equation: _____

2. The product of the first number and 3 is equal to the second number.

Variable(s): _____

Equation: _____

Demonstration Practice (cont.)

3. The quotient of the first number and 2 is equal to the second number.

Variable(s): _____

Equation: _____

4. The second number is 3 less than the first number.

Variable(s): _____

Equation: _____

Practice

Pair Practice

For the following situation, work with your partner to define each variable and then match each verbal situation to the correct equation.

Verbal Description

Equation

- 1.** The quotient of the first number and 9 is equal to the second number.

A $a = b + 9$

$a =$ _____

$b =$ _____

- 2.** The difference of the number and 9 equals the second number.

B $\frac{a}{9} = b$

$a =$ _____

$b =$ _____

- 3.** A number is equal to 9 more than the second number.

C $a - 9 = b$

$a =$ _____

$b =$ _____

Name: _____

I ndependent Practice

Score: _____ / 12 correct

For the following situation, define each variable and then match each verbal situation to the correct equation. Each problem is worth 3 points.

Verbal Description

Equation

1. The difference between two numbers is 2.

A $\frac{a}{2} = b$

$a =$ _____

$b =$ _____

2. The quotient of the first number and 2
is equal to the second number.

B $b = a + 2$

$a =$ _____

$b =$ _____

3. The second number is 2 more than
the first number.

C $a - b = 2$

$a =$ _____

$b =$ _____

4. The product of the number and 2
is equal to the second number.

D $2a = b$


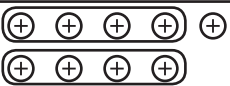
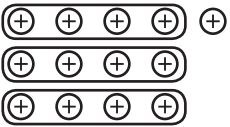
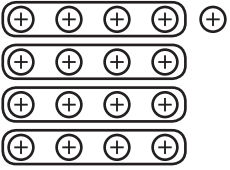
$a =$ _____

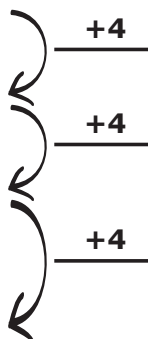
$b =$ _____

Cumulative Review Practice

Score: ____ / 2 correct

1. Use the completed table to answer the following question.

Term	Thinking Process	Total
1	 $1(4)+1$	5
2	 $2(4)+1$	9
3	 $3(4)+1$	13
4	 $4(4)+1$	17
n		??



Which of the following is the correct generalization of the table's pattern? (1 pt.)

- A** $n + 4$ **C** $4n$
B $4n + 1$ **D** $5n + 1$

2. Read the following situations and select the equation that represents the relationship given in the word problem. (1 pt.)

The product of the first number and 12 is equal to the second number.
 a = the value of the first number. b = the value of the second number.

- A** $12b = a$ **C** $12a = b$
B $a \cdot b = 12$ **D** $12 - a = b$

Demonstration Practice

For the following situation, define the variables that are appropriate and write an equation to describe the relationship.

1. The second number is 5 more than twice the first number.

Variable(s): _____

Equation: _____

2. Double the first number is equal to the difference of the second number and 1.

Variable(s): _____

Equation: _____

3. The quotient of the first number and 3 plus 7 is the second number.

Variable(s): _____

Equation: _____

4. The product of the first number and 8 is equal to the sum of the second number and 4.

Variable(s): _____

Equation: _____

P practice

Pair Practice

With your partner, define each variable in the space provided.
Draw a line to match each word problem to the correct equation.
Be prepared to justify your answers.

Verbal Description

Equation

1. Twice the first number minus 6
is equal to the second number.

A $g - d = 6(2)$

$g =$ _____

$d =$ _____

2. The quotient of the first number and 2
is 6 more than the second number.

B $2g - 6 = d$

$g =$ _____

$d =$ _____

3. The difference of the first number and
the second number is equal to the
product of 6 and 2.

C $\frac{g}{2} = d + 6$

$g =$ _____

$d =$ _____

Error Correction Practice

The given situations are work completed by two different students.
Determine which student is incorrect and explain the error.

Write the equation from the given verbal description.

*The product of the first number and 5 is equal to
3 less than the second number.*

Student 1:

$$5x = y - 3$$

Student 2:

$$5 + x = 3 - y$$

Name: _____

Independent Practice

Score: _____ / 12 correct

Define each variable in the space provided. Draw a line to match each word problem to the correct equation. Be prepared to justify your answers. Each problem is worth 3 points.

Verbal Description

Equation

1. 5 added to triple the first number
is the second number.

A $5f = h - 3$

$f =$ _____

$h =$ _____

2. The first number times 5 is 3 less
than the second number.

B $f + 3h = 5$

$f =$ _____

$h =$ _____

3. The sum of the first number and
triple the second number is 5.

C $3f + 5 = h$

$f =$ _____

$h =$ _____

4. The quotient of the first number
and 5 is equal to the difference
of the second number and 3.

D $\frac{f}{5} = h - 3$

$f =$ _____

$h =$ _____

Cumulative Review Practice

Score: ____ / 2 correct

Read the following situations and select the equation that represents the relationship given in the word problem.

1. The sum of the first number and 15 is equal to the second number. (1 pt.)

f = the value of the first number.

s = the value of the second number.

A $15 + s = f$

B $15 + f = s$

C $s + f = 15$

D $15 - f = s$

2. The product of the first number and 6 is equal to the difference of the second number and 2. (1 pt.)

f = the value of the first number.

s = the value of the second number.

A $6 - s = 2f$

B $6 - f = 2s$

C $6f = s - 2$

D $6s = f - 2$

Demonstration Practice

Independent and Dependent

When 2 quantities vary together, there is an independent variable and a dependent variable.

Independent Variable	Dependent Variable

Read the following situations and identify the 2 quantities that vary and the independent and dependent variables.

- Every day I eat pizza in the cafeteria. The cost of my lunch varies, or changes based on how many slices of pizza I buy.

p = the number of slices of pizza I buy
 c = the total cost of my lunch

_____ depends on _____

Independent variable _____

Dependent variable _____

Demonstration Practice (cont.)

2. Sandra has a job passing out flyers for a sandwich shop. The total number of flyers that she passes out each day is determined by the number of people that walk by her that day.

_____ = the number of people that walk by

_____ = the total number of flyers passed out

_____ depends on _____

Independent variable _____

Dependent variable _____

3. Jonathan is trying to make money by washing cars in his neighborhood. The number of cars that he washes will determine how much money that he makes.

_____ = the total amount of money made

_____ = the number of cars washed

_____ depends on _____

Independent variable _____

Dependent variable _____

P practice

Pair Practice

Read the following situations and work with your partner to identify the 2 quantities that vary and the independent and dependent variables.

1. Marisol is putting money away each month to save for a vacation.

Every month she puts \$25 in her savings account.

_____ = the total amount of money saved

_____ = the number of months

_____ depends on _____

2. Sara is trying to figure out her final grade in Mr. Reed's math class.

Each student gets a final grade based on the number of assignments that they turn in.

_____ = the number of assignments turned in

_____ = the final grade

_____ depends on _____

Name: _____

Independent Practice

Score: _____ / 12 correct

Read the following situations. Choose a variable to represent each quantity and label as independent or dependent. Each problem is worth 4 points.

1. Jose just got a summer job where the total amount of money he makes each paycheck will be based on how many hours that he works.

_____ = the number of hours that Jose works

_____ = the amount of money Jose makes

2. Mark drives his car a lot for work and frequently needs to change the oil in his car. The number of oil changes that Mark's car needs each year is determined by how many miles he drove that year.

_____ = the number of oil changes Mark's car needs

_____ = the number of miles driven

3. Angelica is having a party for her birthday. The number of people that come to the party will determine how many pizzas that she will order.

_____ = the number of pizzas that Angelica orders

_____ = the number of people that come to the party

Cumulative Review

Score: ____ / 5 correct

Read the following situation and select the equation that represents the relationship given in the word problem. (1 pt.)

1. *The product of the first number and 6 is equal to the quotient of 24 and a second number.*

f = the value of the first number

s = the value of the second number

A $6f = 24 + s$

C $f + 6 = 24s$

B $6 + s = 24 - f$

D $6f = 24 \div s$

Read the following situation and label each quantity that varies as independent or dependent. (4 pts.)

2. *The total amount of money that Aldo spends on gas each month is determined by the number of miles that he drives that month.*

_____ = the number of miles driven each month

_____ = the total amount of money spent on gas

Demonstration Practice

1. Word Problem:	Define Variable(s):
<p>Alicia works at an electronic store where she makes \$11 each hour.</p> <p>Find the total amount of money Alicia makes.</p>	<p>Let the variable _____ stand for _____</p> <p>_____</p> <p>Let the variable _____ stand for _____</p> <p>_____</p>
Write an Equation:	
<p>Write an equation that can be used to find the total amount of money that Alicia makes based on how many hours that she works.</p> <div style="display: flex; align-items: center; justify-content: center; margin-top: 20px;"> <div style="border: 1px solid black; padding: 10px; width: 30%; text-align: center;"> <u>Calculate the money earned</u> </div> <div style="margin: 0 10px;">=</div> <div style="border: 1px solid black; padding: 10px; width: 30%; text-align: center;"> <u>Total money made</u> </div> </div>	

Demonstration Practice (cont.)

2. Word Problem:	Define Variable(s):
<p>The total cost of shipping a package is \$2 per pound.</p> <p>Find the total cost of shipping a package.</p>	<p>Let the variable _____ stand for _____</p> <p>_____</p> <p>Let the variable _____ stand for _____</p> <p>_____</p>
Write an Equation:	
<p>Write an equation that can be used to find the total cost of a package based on its weight.</p> <div style="display: flex; align-items: center; justify-content: center; margin-top: 20px;"> <div style="border: 1px solid black; padding: 10px; text-align: center; width: 30%;"> <u>Calculate the package shipping cost</u> </div> <div style="margin: 0 10px;">=</div> <div style="border: 1px solid black; padding: 10px; text-align: center; width: 30%;"> <u>Total cost</u> </div> </div>	

Demonstration Practice (cont.)

3. Word Problem:	Define Variable(s):
<p>Stephen is saving up to buy a car. He is putting \$40 per month in his savings account. Find the total amount Stephen has saved.</p>	<p>Let the variable _____ stand for _____</p> <p>_____</p> <p>Let the variable _____ stand for _____</p> <p>_____</p>
Write an Equation:	
<p>Write an equation that can be used to find the total amount of money that Stephen saves based on the number of months he has saved for.</p> <div style="display: flex; align-items: center; justify-content: center; margin-top: 20px;"> <div style="border: 1px solid black; width: 300px; height: 100px; display: flex; align-items: center; justify-content: center;"> <u>Calculate the savings</u> </div> <div style="margin: 0 20px;">=</div> <div style="border: 1px solid black; width: 300px; height: 100px; display: flex; align-items: center; justify-content: center;"> <u>Total savings</u> </div> </div>	

P practice

Pair Practice

For each of the following situations, work with your partner to define the variables and write the equation to represent the situation.

Jorge went to the carnival with his friend. The carnival charges \$3 per ride. Jorge needs to figure out how much money he will spend at the carnival based on the number of rides he takes.

1. Determine and define the variables:

Let the variable _____
stand for _____

Let the variable _____
stand for _____

2. Based on the variables you defined above, write an equation to represent the carnival situation above.

<u>Calculate the ride cost</u>	=	<u>Total Carnival cost</u>
--------------------------------	---	----------------------------

Name: _____

Independent Practice

Score: _____ / 4 correct

Read the following word problems and find the matching equation that represents the relationship. Each match is worth 1 point.

- 1.** Sally works at a cell phone store where she earns \$15 commission for every cell phone (c) that she sells. Find the equation for the total (t) money made. _____ **A** $t = 3c$
- 2.** The cost (c) of the membership to a gym is \$15 per month (t). Find the equation for the total cost for t months. _____ **B** $c = 3t$
- 3.** A DVD club charges \$3 per DVD (c). Find the equation for the total (t) cost of the DVD club per month. _____ **C** $c = 15t$
- 4.** The cost (c) of renting a canoe is \$3 per hour (t). Find the equation for the total cost for renting a canoe t hours. _____ **D** $t = 15c$

Cumulative Review

Score: ____ / 3 correct

1. Read the following situation. Label each quantity that varies as independent or dependent. (2 pts.)

Amirali was organizing a dinner party for his company. The number of people who attend the function will determine the cost for the dinner party.

p = the number of people attending

c = the cost of the dinner party

2. For the following word problem select the equation that represents the relationship. (1 pt.)

The neighborhood butcher is having a sale on steaks. The butcher is selling steaks for \$5 per pound (p). Find the equation for the total cost (t) of buying steaks based on the number of pounds.

A $t = 5p$

B $p = 5 + t$

C $p = 5t$

D $t = 5 + p$

Demonstration Practice

For each of the following situations, define and describe the variables, create an equation and a table representation.

1. Word Problem:	Define Variable(s):												
Midori is saving up to buy a car. Her account has an initial balance of \$300 and she is depositing \$40 per month into her account. Find an equation to represent the amount Midori has saved.	Let the variable _____ stand for _____ Let the variable _____ stand for _____ 												
Write an Equation:	Make a Table:												
<p>Write an equation that can be used to find the balance in Midori's account based on how long she has saved.</p> <div style="display: flex; align-items: center; justify-content: center; margin-top: 20px;"> <div style="border: 1px solid black; padding: 5px; text-align: center; width: 100px;">Amount Deposited</div> <div style="margin: 0 10px;">+</div> <div style="border: 1px solid black; padding: 5px; text-align: center; width: 100px;">Initial Balance</div> <div style="margin: 0 10px;">=</div> <div style="border: 1px solid black; padding: 5px; text-align: center; width: 100px;">Total Saved</div> </div>	<p>Use the table to find out how much money Midori has saved for the different number of months.</p> <div style="margin-top: 20px;"> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td style="width: 25%; height: 30px;"></td><td style="width: 50%;">Process</td><td style="width: 25%; height: 30px;"></td></tr> <tr> <td style="height: 30px;"></td><td></td><td></td></tr> <tr> <td style="height: 30px;"></td><td></td><td></td></tr> <tr> <td style="height: 30px;"></td><td></td><td></td></tr> </table> </div>		Process										
	Process												

Demonstration Practice (cont.)

2. Word Problem:	Define Variable(s):												
<p>The cost of a taxi ride in Chicago is \$0.50 per mile plus an additional fee of \$5.</p> <p>Find the total cost of a taxi ride.</p>	<p>Let the variable _____ stand for _____</p> <p>_____</p> <p>Let the variable _____ stand for _____</p> <p>_____</p>												
Write an Equation:	Make a Table:												
<p>Write an equation that can be used to find the total cost of a taxi ride based on the distance traveled.</p> <div style="display: flex; align-items: center; justify-content: center; margin-top: 20px;"> <div style="border: 1px solid black; padding: 10px; text-align: center; width: 100px;">Total Cost</div> <div style="margin: 0 10px;">=</div> <div style="border: 1px solid black; padding: 10px; text-align: center; width: 100px;">Cost of Miles</div> <div style="margin: 0 10px;">+</div> <div style="border: 1px solid black; padding: 10px; text-align: center; width: 100px;">Initial Fee</div> </div>	<p>Use the table to find out how much a taxi ride costs for different distances traveled.</p> <table border="1" style="margin-top: 20px; width: 100%; border-collapse: collapse;"> <tr> <td style="width: 30%;"></td><td style="width: 40%; text-align: center;">Process</td><td style="width: 30%;"></td></tr> <tr><td></td><td></td><td></td></tr> <tr><td></td><td></td><td></td></tr> <tr><td></td><td></td><td></td></tr> </table>		Process										
	Process												

Demonstration Practice (cont.)

3. Word Problem:	Define Variable(s):															
<p>Johanna is planning a trip and will rent a car. The cost of renting a car is \$10 per day plus the initial fee of \$25. Find the total cost of a rental car.</p>	<p>Let the variable _____ stand for _____</p> <p>Let the variable _____ stand for _____</p>															
Write an Equation:	Make a Table:															
<p>Write an equation that can be used to find the total rental cost based on how long Johanna rents the car.</p> <div style="display: flex; align-items: center; justify-content: center; margin-top: 20px;"> <div style="border: 1px solid black; padding: 5px; text-align: center; width: 100px;">Cost of Days</div> <div style="margin: 0 10px;">+</div> <div style="border: 1px solid black; padding: 5px; text-align: center; width: 100px;">Initial Fee</div> <div style="margin: 0 10px;">=</div> <div style="border: 1px solid black; padding: 5px; text-align: center; width: 100px;">Total Cost</div> </div>	<p>Use the table to find out the total cost for different number of days.</p> <table border="1" style="margin-top: 20px; width: 100%; border-collapse: collapse;"> <tr> <th style="width: 20%;"></th><th style="width: 60%;">Process</th><th style="width: 20%;"></th></tr> <tr><td> </td><td> </td><td> </td></tr> <tr><td> </td><td> </td><td> </td></tr> <tr><td> </td><td> </td><td> </td></tr> <tr><td> </td><td> </td><td> </td></tr> </table>		Process													
	Process															

P

actice

Pair Practice

With a partner, define and describe the variables, circle the letter for the correct equation and table representation.

Peter signed up for a new cell phone plan. His plan each month will cost him \$35 plus \$0.10 per minute.

Define and describe variables to represent each of the unknown values:

1. The equation that represents the situation is:

- A** $c = 0.10m + 35$ **C** $m = 0.10c + 35$
- B** $c = 35.10m$ **D** $c + 35 = 0.10m$

2. The table that represents the situation is:

A

Number of minutes (m)	Total phone bill cost (c)
20	55
50	85
100	135

C

Number of minutes (m)	Total phone bill cost (c)
55	20
85	50
135	100

B

Number of minutes (m)	Total phone bill cost (c)
37	20
40	50
45	100

D

Number of minutes (m)	Total phone bill cost (c)
20	37
50	40
100	45

Error Correction Practice

The given situation is work completed by a student. Determine the error in the students work and explain your reasoning.

For the given situation, write the equation and complete a table.

Isabella rented a motor scooter for the day. To rent a scooter, it costs \$20 plus an additional \$10 an hour.

$$c = 10 + 20h$$

Hours Rented (<i>h</i>)	Total Cost (<i>c</i>)
1	30
2	50
3	70

Name: _____

Independent Practice

Score: ____ / 2 correct

For the following situation, circle the correct equation and table representation.

George signed up for a new cable plan. Each month, he is charged a \$50 fee, plus \$5 per movie package. Find George's total cost for cable.

1. The equation that represents the situation is: (1 pt.)

A $c = m + 50$

C $c = 50m$

B $c = 5m + 50$

D $c = 50m + 5$

2. The table that represents the situation is: (1 pt.)

A

Movie packages(m)	cost (c)
1	50
2	55
3	60

C

Movie packages(m)	cost (c)
1	55
2	60
3	65

B

Movie packages(m)	cost (c)
1	50
2	100
3	150

D

Movie packages(m)	cost (c)
1	5
2	55
3	105

Cumulative Review

Score: ____ / 3 correct

1. Read the following word problem and select the equation that represents the relationship. (1 pt.)

The cost (c) of renting a bike to tour downtown is \$15 per hour (h).

Find the equation for the total cost for renting a bike.

- A** $c = h + 15$ **C** $h = 15c$
B $h = c + 15$ **D** $c = 15h$

Use the following word problem to answer questions 2 and 3.

Nikita is planning the company summer party. The party will cost (c) \$6 per person (p) plus a rental fee of \$65 for setup services.

2. Select the equation that represents the word problem. (1 pt.)

- A** $c = 65p + 6$ **C** $c = p + 65$
B $c = 6p + 65$ **D** $c = p + 6$

3. Select the table that represents the word problem. (1 pt.)

A

Number of People (p)	Total Cost (c)
1	71
2	77
3	83

C

Number of People (p)	Total Cost (c)
1	65
2	71
3	77

B

Number of People (p)	Total Cost (c)
1	71
2	136
3	201

D

Number of People (p)	Total Cost (c)
1	66
2	67
3	68

Demonstration Practice

For each of the following situations, define and describe the variables, create an equation and a table representation.

1. Word Problem:	Define Variable(s):												
<p>Margret is selling cups of lemonade to earn money. She already has \$5 and is selling the lemonade for \$1.50 per cup.</p> <p>Find the total amount of money Margret has.</p>	<p>Let the variable _____ stand for _____</p> <p>_____</p> <p>Let the variable _____ stand for _____</p> <p>_____</p>												
Write an Equation:	Make a Table:												
<p>Write an equation that can be used to find Margret's total amount of money based on the number of cups of lemonade she has sold.</p> <p>_____</p>	<p>Use the table to calculate the varying amount of money Margret made for your selected numbers of cups of lemonade sold.</p> <table border="1" style="margin: 10px auto; border-collapse: collapse; text-align: center;"> <tr> <td style="width: 20%; height: 25px;"></td><td style="width: 60%; height: 25px;">Process</td><td style="width: 20%; height: 25px;"></td></tr> <tr> <td style="height: 25px;"></td><td style="height: 25px;"></td><td style="height: 25px;"></td></tr> <tr> <td style="height: 25px;"></td><td style="height: 25px;"></td><td style="height: 25px;"></td></tr> <tr> <td style="height: 25px;"></td><td style="height: 25px;"></td><td style="height: 25px;"></td></tr> </table>		Process										
	Process												

Demonstration Practice (cont.)

2. Word Problem:	Define Variable(s):												
<p>Lilia wants to rent a motor scooter. To rent a scooter it costs \$0.30 per mile, plus an initial fee of \$45. Find the total cost to rent a scooter.</p>	<p>Let the variable _____ stand for _____</p> <p>Let the variable _____ stand for _____</p>												
Write an Equation:	Make a Table:												
<p>Write an equation that can be used to find the total cost of renting a motor scooter based on the number of miles driven.</p> <p>_____</p>	<p>Use the table to calculate the varying costs to rent a scooter for your selected numbers of miles driven.</p> <table border="1" style="margin: 10px auto; border-collapse: collapse; text-align: center;"> <tr> <td style="width: 15%; height: 25px;"></td><td style="width: 60%;">Process</td><td style="width: 25%; height: 25px;"></td></tr> <tr> <td style="height: 25px;"></td><td></td><td></td></tr> <tr> <td style="height: 25px;"></td><td></td><td></td></tr> <tr> <td style="height: 25px;"></td><td></td><td></td></tr> </table>		Process										
	Process												

Demonstration Practice (cont.)

3. Word Problem:	Define Variable(s):												
<p>Lorenzo joined a soccer league for \$20. Lorenzo pays \$5 for each game he plays.</p> <p>Find the total cost to play on the soccer league.</p>	<p>Let the variable _____ stand for _____</p> <p>Let the variable _____ stand for _____</p>												
Write an Equation:	Make a Table:												
<p>Write an equation that can be used to find the total cost for Lorenzo to play soccer based on the number of games he plays.</p> <p>_____</p>	<p>Use the table to calculate the varying total costs for the league for your selected numbers of soccer games played.</p> <table border="1" style="margin: 10px auto; border-collapse: collapse; text-align: center;"> <tr> <td style="width: 20%; height: 25px;"></td><td style="width: 60%;">Process</td><td style="width: 20%; height: 25px;"></td></tr> <tr> <td style="height: 25px;"></td><td></td><td></td></tr> <tr> <td style="height: 25px;"></td><td></td><td></td></tr> <tr> <td style="height: 25px;"></td><td></td><td></td></tr> </table>		Process										
	Process												

P practice

Pair Practice

With a partner, define and describe the variables, circle the letter for the correct equation and table representation.

At a local copy shop, it costs \$0.50 per page of colored copy plus an initial processing fee of \$4. Find the cost of making color copies.

Define and describe variables to represent each of the unknown values:

1. The equation that represents the situation is:

- A** $p = 0.50c + 5$ **C** $c = 0.50p + 4$
- B** $c + 4 = 0.50p$ **D** $c = 4.50p$

2. The table that represents the situation is:

A

Number of Pages (p)	Total Copy Cost (c)
5	2
7	6
9	10

C

Number of Pages (p)	Total Copy Cost (c)
2	9
6	27
10	45

B

Number of Pages (p)	Total Copy Cost (c)
2	5
6	7
10	9

D

Number of Pages (p)	Total Copy Cost (c)
2	4.50
6	5.50
10	8

Error Correction Practice

The given situations are work completed by two different students. Determine which student is incorrect and explain the error(s).

Given the following contextual situation, write an equation to describe the relationship between the quantities that vary.

Marie and Joanna are renting a canoe. The canoe rental costs a flat fee of \$7 plus \$5 per hour (h). Find the equation for the total cost (c).

Student 1:

$$7h + 5 = c$$

Student 2:

$$7 + 5h = c$$

Name: _____

Independent Practice

Score: _____ / 2 correct

For the following situation, circle the correct equation and table representation.

Amir is purchasing a pizza from a local shop. The pizza costs \$12 plus \$0.50 for each topping. Find the cost of a pizza.

1. The correct equation is: (1 pt.)

A $c = t + 12$

C $c = 12.50t$

B $c = 12t + 0.50$

D $c = 0.50t + 12$

2. The correct table is: (1 pt.)

A

Number of Toppings (t)	Cost of a Pizza (c)
1	13.50
2	14.00
3	14.50

C

Number of Toppings (t)	Cost of a Pizza (c)
1	12.50
2	13.00
3	13.50

B

Number of Toppings (t)	Cost of a Pizza (c)
1	12.00
2	13.00
3	14.00

D

Number of Toppings (t)	Cost of a Pizza (c)
1	12.50
2	24.00
3	36.50